CHAPTER - 1 *EQUILIBRIUM OF FORCES*

1.1 MECHANICS

Mechanics is a branch of the physical sciences that is concerned with the state of rest or motion of bodies that are subjected to the action of forces. In general, this subject can be subdivided into three branches: rigid-body mechanics, deformable-body mechanics, and fluid mechanics. Rigid-body mechanics is divided into two areas: statics and dynamics. *Statics* deals with the equilibrium of bodies, that is, those that are either at rest or move with a constant velocity; whereas dynamics is concerned with the accelerated motion of bodies.

1.1.1 Matter

Anything which has mass and occupy space is called matter. Generally, it has three phases

- 1. Solid
- 2. Liquid
- 3. Gas

Solid $\xrightarrow{\text{Heat}} Liquid \xrightarrow{\text{Heat}} Gas \xrightarrow{\text{Heat}} Plasma$ Fluid Mechanics

1.1.2 Particle

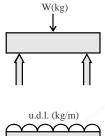
A particle has a mass, but a size that can be neglected. For example, the size of the earth is insignificant compared to the size of its orbit, and therefore the earth can be modeled as a particle when studying its orbital motion. When a body is idealized as a particle, the principles of mechanics reduce to a rather simplified form since the geometry of the body will not be involved in the analysis of the problem.

1.1.3 Rigid Body

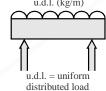
A rigid body can be considered as a combination of a large number of particles in which all the particles remain at a fixed distance from one another, both before and after applying a load. This model is important because the material properties of anybody that is assumed to be rigid will not have to be considered when studying the effects of forces acting on the body. In most cases the actual deformations occurring in structures, machines, mechanisms, and the like are relatively small, and the rigid-body assumption is suitable for analysis.

1.1.4 Concentrated Force A concentrated force represents the effect of a loading which is assumed to act at a point on a body. We can represent a load by a concentrated force, provided the

(i) Concentrated Force

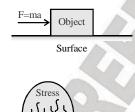


(ii) Distributed Force



3. According to the Effect produced by the Force

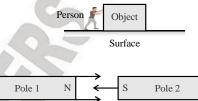
(i) External Forces



(ii) Internal Forces

- 4. Classification According to Application of Force
- (i) Contacting Force

(ii) Non Contacting Force

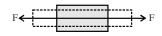


Object

- 5. Classification According to Nature of Stress Produced

S

(i) Tensile Force

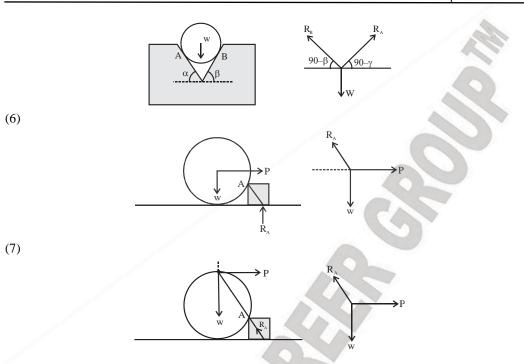


(ii) Compressive Force



(iii) Shearing Force

Ν



1.3.6 Principle of Physical independence of Forces

Each force is having its own effect and is independent of the presence of other forces. This principle is applicable in all engineering problems in which a number of forces are acting on a body.

1.3.7 Equilibrium of Forces

- 1. Equal in magnitude
- 2. Act along the same straight line
- 3. Are opposite in direction
- 4. Resultant force is zero.

1.3.8 Law of Super Position

According to this law there will be no effect on the action of a given system of forces acting on a rigid body if added or subtracted from them another system of forces which is also in equilibrium.

1.3.9 Principle of Transmissibility of Forces

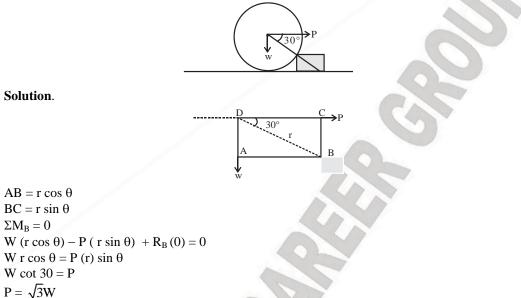
Principle of Transmissibility of forces may be stated in other words as; A force acting at any point of a rigid body may be considered to act at any other point in its line of action provided the latter point is either one of the points of the body or rigidly connected with it.

1.3.10 Laws of Forces 1. Resultant of Coplanar Forces

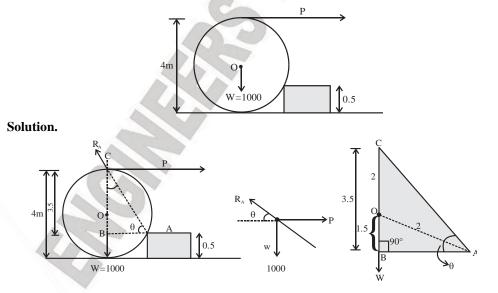
$$\frac{F_{A}}{\sin \alpha} = \frac{F_{B}}{\sin \beta} = \frac{F_{C}}{\sin \gamma}$$

1.8 NUMERICALS

Example. For the given configuration, force P acting horizontally is pulling out a roller out of ditch. Find the minimum force P in terms of W.



Example. For the given configuration, force P acting horizontally is pulling out a roller out of ditch. Find the minimum force P to take out the roller out of ditch.



4. Square c/s with diagonal horizontal,
$$Z = \frac{a^3 \sqrt{2}}{6}$$

5. Circular c/s of diameter "d", $Z = \frac{\pi d^3}{32}$

A long diameter "d" is available. It is proposed to cut out a strongest beam from it. Then

$$Z = \frac{b(d^2 - b^2)}{6}$$

Therefore,

$$Z_{\max} = \frac{bd^3}{9} \text{ for } b = \frac{d}{\sqrt{3}}$$

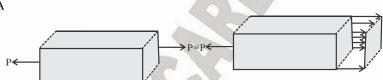
2.3 SIMPLE STRESS STRAIN RELATIONSHIPS

2.3.1 Stress

When a material is subjected to an external force, a resisting force is set up within the component. The internal resistance force per unit area acting on a material or intensity of the forces distributed over a given section is called the stress at a point.

(i) It uses original cross section area of the specimen and also known as engineering stress or conventional stress.

Therefore, $\sigma = \frac{P}{A}$



Where P is expressed in Newton (N) and A, original area, in square meters (m), the stress σ will be expressed in N/m². This unit is called Pascal (Pa).

(ii) As Pascal is a small quantity, in practice, multiples of this unit is used.

 $1 kPa = 10^{3} Pa = 10^{3} N / m^{2}$ $1 MPa = 10^{6} Pa = 10^{6} N / m^{2} = 1N / mm^{2}$ $1 GPa = 10^{9} Pa = 10^{9} N / m^{2}$ (MPa = Mega Pascal) 1 GPa = Giga Pascal)

Let us take an example: A rod 10 mm \times 10 mm cross-section is carrying an axial tensile load 10 kN. In this rod the tensile stress developed is given by

$$(\sigma_1) = \frac{P}{A} = \frac{10kN}{(10mm \times 10mm)} = \frac{10 \times 10^3 N}{100mm^2} = 100 N / mm^2 = 100 MPa$$

The resultant of the internal forces for an axially loaded member is normal to a section cut perpendicular to the member axis.

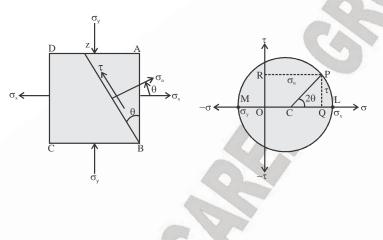
The force intensity on the shown section is defined as the normal stress.



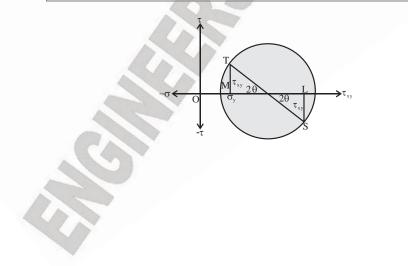
In the examination you only draw final figure (which is in Step-V) and follow the procedure step by step so that no mistakes occur.

Construction of Mohr's circle for unlike stresses (when σ_x and σ_y) are opposite in sign)

Follow the same steps which we followed for construction for 'like stresses' and finally will get the figure shown below

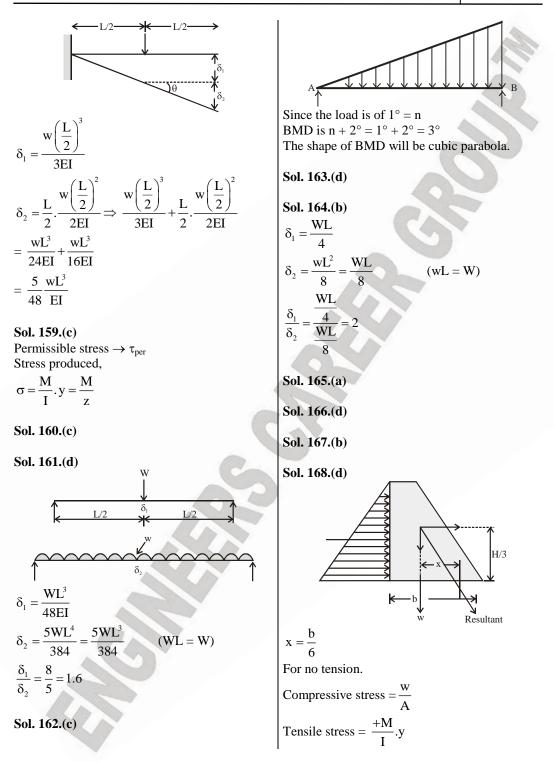


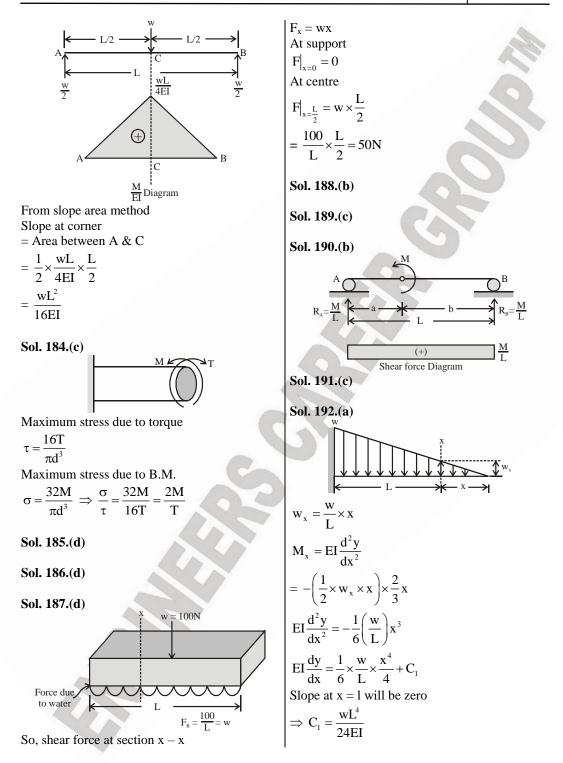
For construction of Mohr's circle for principal stresses when (σ_1 and σ_2 is known) then follow the same steps of constant of Mohr's circle for Bi-axial stress (when only σ_x and σ_y known) just change the $\sigma_x = \sigma_1$ and $\sigma_y = \sigma_2$

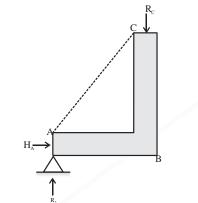


(d) Is supported on all sides throughout its length	(c) Perpendicular(d) Minimum cross-section
144. Which of the following is a dimensionless quantity?(a) Shear force(b) Stress	150. The permanent deformation of concretewith time under steady load is called:(a) Visco-elasticity(b) Vicidity(c) Creep(d) Relaxation
 (c) Strain (d) Modulus of elasticity 145. In a simply supported beam of span, L 	151. Unit of second moment of area is; (a) mm (b) mm^4 (c) mm^3 (d) mm^2
subjected to Uniformly Distributed Load (UDL) of intensity W kN/m over it's entire length the maximum bending is given by the expression: (a) $\frac{WL^2}{8}$ (b) $\frac{WL}{2}$ (c) $\frac{WL^2}{2}$ (d) WL	152. In case of biaxial stress, the maximum value of shear stress is given by(a) Difference of the normal stressed(b) Half the difference of the normal stresses(c) Sum of the normal stresses(d) Half the sum of the normal stresses
146. A simply supported beam of span 'L' is loaded with downward uniformly distributed load of intensity W/m over it's entire length. Which of the following orientation of T-beams is preferred to resist bending	 153. From a circular plate of diameter 6.0 cm , a circle is cut out whose diameter is a radius of the plate. The distance of centre of gravity of the remainder from the centre of circular plate is (a) 2.0 cm (b) 1.5 cm (c) 1.0 cm (d) 0.5 cm
	 154. In a section undergoing pure bending, the neutral surface is subjected to (a) Compression strain (b) Tensile strain (c) Zero strain (d) None of the above
 (d) [147. The ratio of normal stress to normal strain within elastic limits is called: (a) Young's Modulus (b) Shear Modulus (c) Poisson's Ratio (d) Bulk Modulus 	 155. The ability of a material to absorb energy till the breaking or rupture takes place is known as (a) Hardness (b) Toughness (c)Brittleness (d) Softness
 148. The shape of bending Moment Diagram in a beam subjected to only Uniformly Distributed Load (UDL) is: (a) Constant (b) Cubic parabola (c) Parabola (d) Triangular 	156. At the point of contraflexure(a) Bending moment is minimum(b) Bending moment is maximum(c) Bending moment is zero(d) Bending moment is zero and its sign changes
149. Compression members always tend to buckle in the direction of the:(a) Least radius of gyration(b) Axis of load	157. The shear diagram for a cantilever beam subjected to a concentrated loads at the free end is given by a/an(a) Triangle(b) Rectangle

230. An open ended thin cylindrical shell,	236. A cantilever of span ' ℓ ' has a load P acting
subjected to a uniform internal pressure will be	at the free end. The bending moment at free end
subjected to	will be
(a) Hoop stress only	(a) 0 (b) P
(b) Longitudinal stress only	
(c) Both hoop stress and longitudinal stress	$(c) - P \qquad (d) \frac{P}{2}$
(d) None of the above	2
231. Moment of inertia is a concept applicable	237. Consider the following statements:
in case of	A simply supported beam is subjected to a
(a) A rotating body	couple somewhere in the span. It would produce
(b) A body moving in a straight line	 A rectangular SF diagram Parabolic B < diagrams
(c) A body at rest	3. Both + ve and $-ve$ BM which are maximum
(d) both (a) and (b) (Column setting not proper)	at the point of application of the couple.
222 When shands makin in a schumm liss	Of these statements:
232. When slenderness ratio in a column lies between $22 \text{ to } 120$ it is become as	(a) 1, 2 and 3 are correct
between 32 to 120, it is known as (a) Long column (b) Short column	(b) 1 and 2 are correct
(a) Long column(b) Short column(c) Medium column(d) Stocky column	(c) 2 and 3 are correct
(c) Medium column (d) Stocky column	(d) 1 and 3 are correct
233. Every material obeys. Hooke's law within	(d) I and 5 are concer
its	238. A beam simply - supported at both the
(a) Elastic limit	ends, of length 'L' carries two equal unlike
(b) Plastic limit	couples 'M' at two ends. If the flexural rigidity
(c) Limit of proportionality	EI is constant, then the central deflection of
(d) None of the above	beam is given by
234. If a uniform bar is supported at one end in	(a) $\frac{ML^2}{4EI}$ (b) $\frac{ML^2}{16EI}$ (c) $\frac{ML^2}{64EI}$ (d) $\frac{ML^2}{8EI}$
a vertical direction and loaded at the bottom end	
by a load equal to the weight of the bar, the	(c) $\frac{ML^2}{64EL}$ (d) $\frac{ML^2}{8EL}$
strain energy as compared to that due to self	64EI 8EI
weight will be	
(a) Same (b) Half	239. Euler's crippling load for a column of
(c) Twice (d) Thrice	length with one end fixed and the other hinged
	is
225 East a since material if E N and 1	$\pi^2 EI$ $\pi^2 EI$
235. For a given material, if E, N and $\frac{1}{m}$ are	(a) $\frac{\pi^2 \text{EI}}{\text{L}^2}$ (b) $\frac{4\pi^2 \text{EI}}{\text{L}^2}$
young's Modulus, modulus of Rigidity and	
Poisson's Ratio then	(c) $\frac{\pi^2 \text{EI}}{4 \text{I}_{\perp}^2}$ (d) $\frac{2\pi^2 \text{EI}}{\text{I}_{\perp}^2}$
$() = \alpha y (1, 1)$ $() = \alpha y (1, 1)$	4L L
(a) $E = 2N\left(1 + \frac{1}{m}\right)$ (b) $E = 2N\left(1 - \frac{1}{m}\right)$	240. A circular shaft can transmit a torque of 5
201 1	kNm. If the torque is reduced to 4 kNm, then
(c) $E = \frac{2N}{\left(1 + \frac{1}{m}\right)}$ (d) $E = \frac{1}{2N\left(1 + \frac{1}{m}\right)}$	the maximum Value of bending moment that
$(1+\frac{1}{2})$ $2N(1+\frac{1}{2})$	can be applied to the shaft is
	(a) 1 kNm (b) 2 kNm
	(c) 3 kNm (d) 4 kNm







Unstable because all reaction are concurrent

3.5 METHOD OF ANALYSIS(STATICALLY DETERMINATE AND STABLE TRUSS)

There are two methods of analysis for statically determinate and stable trusses. They are:

- 1. Method of Joint
- 2. Method of Section

1. Method of Joint

In a planer-truss, at every joint there are two conditions of equilibrium

$$\Sigma F_{\rm x} = 0$$

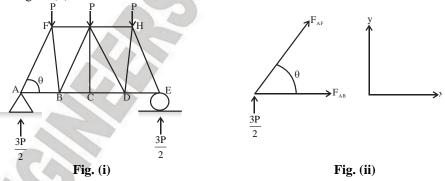
$$\Sigma F_{\rm y} = 0$$

Since all the members at a joint are assumed to pass through a single point, moment about the joint will always be zero. Hence $\Sigma M = 0$ will not be of any consequence.

Sign Convention: Tension (+) ve. Compression (-)ve.

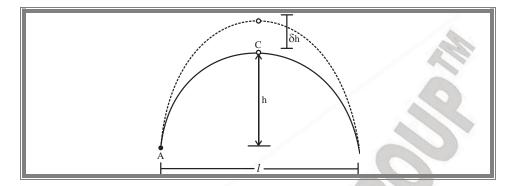
In Method of Joint

Analysis should start at joint having at least one known force and at most two unknown forces. For example in the following figure, if we take joint A then free body diagram of joint A can be drawn as in Figure (ii)



Now from the equilibrium of forces we have

$$\Sigma F_x = 0 \Longrightarrow F_{AB} + F_{AF} \cos \theta = 0$$



3.6.3 ANALYSIS OF STATICALLY DETERMINATE CABLES

Cable is assumed to have zero self weight and BM at every, section is zero.

Steps to Analyse Cable with 2 Supports at Same Level.

i. Find the vertical reaction V_A and V_B by taking moment about one support, similar to that of a simply supported beam.

ii. If there is only vertical loads, then $H_A = H_B$.

iii. If position of any point of chord is known, take $\Sigma M = 0$ about this point to calculate horizontal reaction at supports. Usually we take the lowest point.



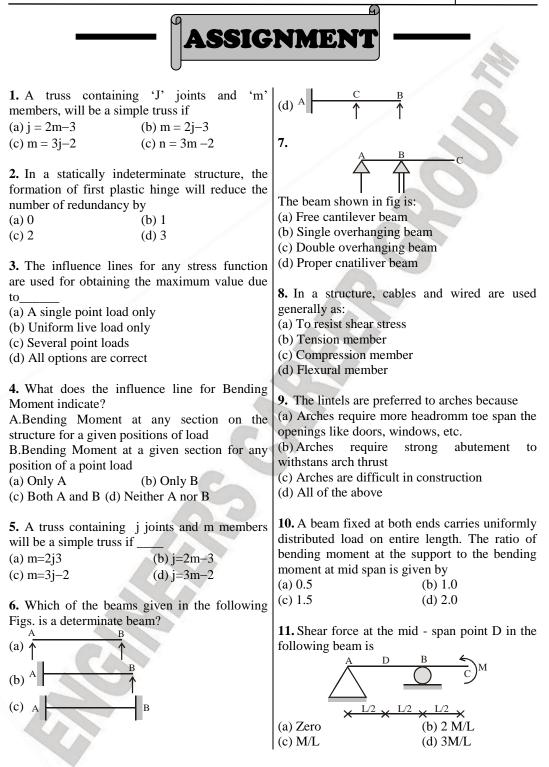
iv. Tension at the segments near to supports equal to resultant forces at support.



We can analyse cable with support at two levels similar to that of 3 hinged arch with support at different levels.

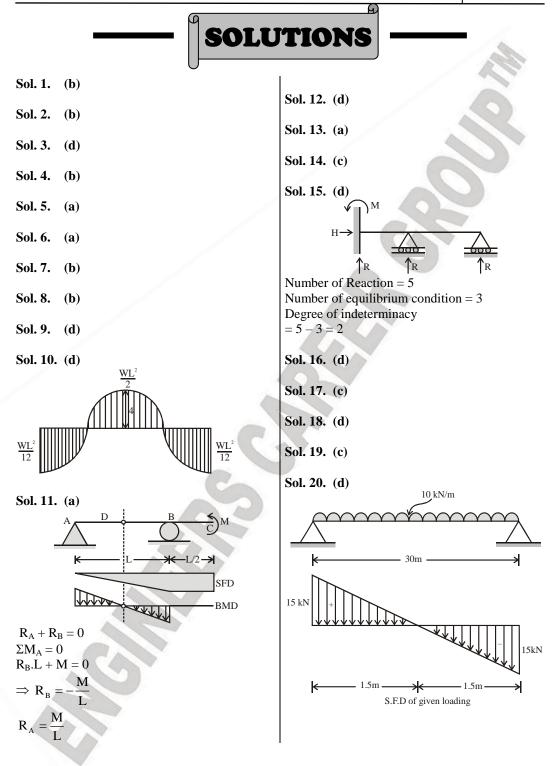
Analysis of cable with UDL all over is length.

$$V_{A} = V_{B} = \frac{w\ell}{z}$$
$$H_{A} = H_{B} = \frac{w\ell^{2}}{8h}$$



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$$A_{u} = \frac{T_{u}S_{1}}{b_{1}d_{1}(0.87f_{x})} + \frac{V_{u}S_{1}}{2.5d_{1}(0.87f_{y})} \qquad i.e. \ (\tau_{ce} - \tau)bd > \frac{0.87f_{y}A_{st}d}{S_{1}}$$

But the total transverse reinforcement shall not be less than $A_{SV} < \frac{(\tau_{ce} - t_v)b.S_1}{0.87f_v}$

Where,

 T_{u} = Ultimate tensional moment

 V_{μ} = Ultimate shear force

 $S_v =$ Spacing of the stirrup reinforcement

 $b_1 = c/c$ distance between corner bars in the direction of width

 $d_1 = c/c$ distance between corner bars in the direction of width

B = Breadth of the member

 $f_v =$ Characteristic strength of shear reinforcement ≤ 415 N/mm²

$$\tau_{ve} = \frac{V_e}{bd} = Equivalent shear stress$$

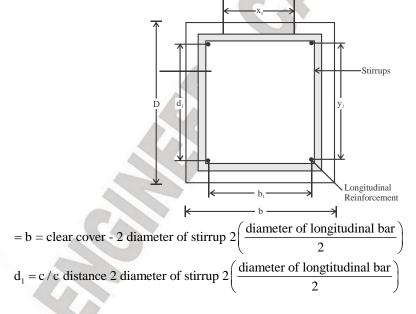
 τ_c = Shear strength of concrete as in table 19 of IS 456.

The transverse reinforcement for torsion shall be rectangular closed stirrups placed perpendicular to the axis of the member. The spacing of the stirrups shall not exceed the least of

 $x_v \frac{x_1 + y_1}{4}$ and 300 mm, where x_1 and y_1 are the short and long dimensions of the stirrups as

shown in figure shown below.

Where $b_1 = c/c$ distance between corner bars in the direction of the width.

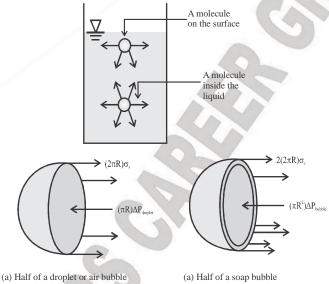


CONCRETE STRUCTURES

(c) Cement provides strength, durability and water tightness to the concrete(d) All options are correct	(a)Flange has adequate reinforcement transverse to beam(b)It is built integrally with the beam(c)It is effectively bonded together with the
156. The produce impermeable	beam
concrete	(d)All options are correct
(a) Thorough mixing of concrete is required	
(b) Proper compaction of concrete is required	163.Pickup the incorrect statement from the
(c) Proper curing of concrete is required	following: Tensile reinforcement bars of a
(d) All options are correct	rectangular beam
	(a)Are curtailed if not required to resist the
157. The entrained air in concrete	bending moment
(a) Increase workability	(b)Are bent up at suitable places to serve as
(b) Decreases workability	shear reinforcement
(c) Decreases resistance to weathering	(c)Are bent down at suitable places to serve as
(d) Increase strength	shear reinforcement
470 71	(d)Are maintained at bottom to provide at least
158. The neutral axis of a T-beam exists	local bond stress
(a) Within the flange	
(b) At the bottom edge of the slab	164.In a single reinforced beam, if the
(c) Below the slab	permissible stress in concrete reaches earlier
(d) All options are correct	than that in steel, the beam section is called
	(a) Under-reinforced section
159. The width of the rib of a T-beam is	(b) Over reinforced section
generally kept between	(c) Economic section
(a) 1/7 to 1/3 of rib depth	(d) Critical section
(b) $1/3$ to $\frac{1}{2}$ of rib depth	
(c) $\frac{1}{2}$ to $\frac{3}{4}$ of rib depth	165. The width of the flange of a T-beam, which
(d) 1/3 to 2/3 of rib depth	may be considered to act effectively with the rib
	depends upon
160.For the design of a simply supported T-	(a) Breadth of the rib
beam the ratio of the effective span to the	(b) Overall thickness of the rib
overall depth of the beam is limited to	(c) Centre to centre distance between T-beam
(a) 10 (b) 15	(d) All options are correct
(c) 20 (d) 25	
	166. The minimum thickness of the cover at the
161. Though the effective depth of a T-beam is	end of a reinforcing bar should not be less than
the distance between the top compression edge	twice the diameter or the bar subject to a
to the centre of the tensile reinforcement for	minimum of
heavy loads it is taken as	(a) 10mm (b) 15mm
(a) $1/8^{th}$ of span (b) $1/10^{th}$ of span (c) $1/12^{th}$ of span (d) $1/16^{th}$ of span	(c) 20mm (d) 25mm
(c) $1/12^{th}$ of span (d) $1/16^{th}$ of span	
	167. Minimum spacing between horizontal
162.A part of the slab may be considered as the	parallel reinforcement of different sizes, should
flange of the T-beam if	not be less than
	(a)One diameter of thinner bar
	(b)One diameter of thicker bar

force that causes this tension acts parallel to the surface and is due to the attractive forces between the molecules of the liquid. The magnitude of this force per unit length is called surface tension or coefficient of surface tension σ_s and is usually expressed in the unit N/m. This effect is also called surface energy (per unit are) and is expressed in the equivalent unit of N.m/m².

The attractive forces applied on the interior molecule by the surrounding molecules balance each other because of symmetric, and the attractive forces applied by the gas molecules above are usually very small. Therefore, these is a net attractive force acting on the molecule at the surface of the liquid, which tends to pull the molecules on the surface toward the interior of the liquid. This force is balanced by the repulsive forces from the molecules below the surface that are trying to be compressed. The result is that the liquid minimizes its surface area. This is the reason for the tendency of liquid droplets to attain a spherical shape. Which has the minimum surface area for a given volume.



The free – body diagram of half of a droplet or air bubble and half of a soap bubble.

Attractive forces acting on a liquid molecule at the surface and deep inside the liquid. Droplet $(2\pi R)\sigma_s = (\pi R^2)\Delta P_{droplet}$

$$\begin{split} \Delta P_{droplet} &= P_{i} - P_{o} = \frac{2\sigma_{s}}{R} \\ Soap \ bubble: \ 2(2\pi R)\sigma_{s} &= (\pi R^{2})\Delta P_{bubble} \\ \Delta P_{bubble} &= P_{i} - P_{o} = \frac{4\sigma_{s}}{R} \end{split}$$

5.1.5 Capillary Effect

Another interesting consequence of surface tension is the capillary effect, which is the rise or fall of a liquid in a small-diameter tube inserted into the liquid. Such narrow tubes or confined flow channels are called capillaries. The rise of kerosene through a cotton wick inserted into the reservoir of a kerosene lamp is due to this effect. The capillary effect is also partially responsible 1. When body is displaced from its original position, and it ends to come back to its original position

- 2. When body is displaced from its original position, it remains in that new position
- 3. When a body is displaced from its original position, it continues to move away

5.2.2 Kinematics of Fluid Flow

The Science which deals with the geometry of motion of fluids without reference to the forces causing the motion is known as hydro kinematics or simply kinematics. Thus kinematics involves merely the description of the motion of fluids in terms of space-time relationship. One the other hand the science which deals with the action of the forces in producing or changing motion of fluids is known as hydro kinematics or simply kinetics.

There are in general two methods by which the motion of a fluid may be described. These are the Lagrangian method and the Eulerian method.

In the Lagrangian method any individual fluid particle is selected, which is pursued throughout its course of motion and the observation is made about the behavior of this particle during its course of motion through space. In the Eulerian method any point in the space occupied by the fluid is selected and observation is made of whatever changes of velocity, density and pressure which take place at that point. Out of these two methods the Eulerian method is commonly adopted in fluid mechanics and therefore the same is used in the following analysis.

5.3 TYPES OF FLUID FLOW

1. Steady Flow

Fluid flow is said to be steady if at any point in the flowing fluid various characteristics such as velocity, pressure, density, temperature etc., which described the behaviors of the fluid in motion, do not change with time.

Thus the steady flow may be expressed mathematically by the following expression at any point in the flowing fluid.

$$\left(\frac{\partial \mathbf{u}}{\partial t}\right) = \mathbf{0}; \left(\frac{\partial \mathbf{v}}{\partial t}\right) = \mathbf{0}; \left(\frac{\partial \mathbf{w}}{\partial t}\right) = \mathbf{0}; \left(\frac{\partial \mathbf{p}}{\partial t}\right) = \mathbf{0}; \left(\frac{\partial \mathbf{p}}{\partial t}\right) = \mathbf{0}$$

(i) Unsteady Flow

Fluid flow is said to be unsteady if at any point in the flowing fluid any one or all the characteristics which describe the behavior of the fluid in motion change with time. Thus a flow of fluid is unsteady, if at any point in the flowing fluid

$$\left(\frac{\partial \mathbf{V}}{\partial t}\right) \neq 0$$
; and or $\left(\frac{\partial \mathbf{p}}{\partial t}\right) \neq 0$ etc.

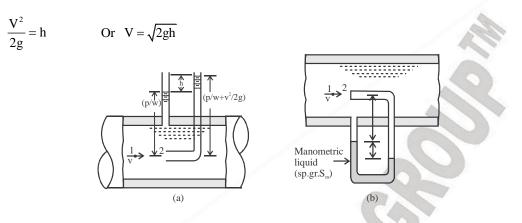
2. Uniform Flow

When the velocity of flow of fluid does not change, both in magnitude and direction, from point to point in the flowing fluid, for any given instant of time, the flow is said to be uniform. In the

mathematical form a uniform flow may therefore be expressed as $\left(\frac{\partial V}{\partial s}\right) = 0$

(i) Non-Uniform Flow

If the velocity of flow of fluid changes from point to point in the flowing fluid at any instant, the flow is said to be non-uniform. In the mathematical form a non-uniform flow may be expressed as



Pilot tube used for measuring velocity in pipes

Consider point 1 slightly upstream of the stagnation point 2 as shown in fig. Applying Bernoullis equation between the points 1 and 2, we get

$$\frac{\mathbf{p}_1}{\mathbf{w}} + \frac{\mathbf{V}^2}{2\mathbf{g}} = \frac{\mathbf{p}_2}{\mathbf{w}}$$

The equation for the pressure through the manometer in meters of water may be written as

$$\frac{p_1}{w}S + yS + xS_m = (y+x)S + \frac{p_2}{w}S$$

Where S and S_m are the specific gravities of the fluid flowing in the pipe and the manometric liquid respectively. By simplifying

$$\frac{\mathbf{p}_2}{\mathbf{w}} - \frac{\mathbf{p}_1}{\mathbf{w}} = \mathbf{x} \left(\frac{\mathbf{S}_{\mathrm{m}}}{\mathbf{S}} - 1 \right)$$

After substituting for $[(p_2/w) - (p_1/w)]$ in Eq. (i) and solving for V,

$$V = \sqrt{2gx\left(\frac{S_m}{S} - 1\right)}$$

Again introducing the coefficient of the pitot tube C, the actual velocity of flow is given by

$$V = C \sqrt{2gx \left(\frac{S_m}{S} - 1\right)}$$

4. Orifice Meter

1. It is used to measure discharge through a pipe

2. In this case a circular plate with concentric sharp edged hole is installed in a pipe such that the plate is perpendicular to the axis of pipe

3. Concept of discharge measurement is same as that in venturimeter but it is a cheaper arrangement as compared to venturimeter

4. In this case, only a small length of pipe is affected hence if there is space restriction, orificemeter can be used in place of venturimeter

5. However, the disadvantage is that the head loss in more in this case due to flow operation. The region where flow area is minimum is called venna –contracta

 a_1 is x –sectional area of section (1)-(1)

Thus for a side slope of 60° , the length of sloping side is equal to the base width of the trapezoidal.

4. Most Economical Triangular Channel Section

As shown in a figure a triangular channel. The side sides are n(horizontal) to 1(vertical)Let, y = Depth of flow, and

 θ = Angle made by the sides with the vertical

From
$$\triangle ODC$$
, $\frac{CD}{DO} = \tan \theta$ or $\frac{CD}{y} = \tan \theta$
or, $CD = y \tan \theta$

Triangular channel

Also, $\frac{DO}{CO} = \cos \theta$ or $\frac{y}{CO} = \cos \theta$ Or, CO = y sec θ

Area of flow,

$$A = \frac{1}{2} \times BC \times DO = \frac{1}{2} \times 2CD \times DO = \frac{1}{2} \times 2y \tan \theta \times y = y^{2} \tan \theta$$

i.e., $A = y^{2} \tan \theta$...(i)
Perimeter, $P = BO + OC = 2OC = 2y \sec \theta$ ($\because BO=OC$) ...(ii)

Substituting the value of $y\left(=\sqrt{\frac{A}{\tan\theta}}\right)$ from equation (i) in equation. (ii), we get

$$P = 2\sqrt{\frac{A}{\tan\theta}\sec\theta} = 2\frac{\sqrt{A}}{\sqrt{\tan\theta}}(\sec\theta) \qquad \dots (iii)$$

Assuming the area to be constant, eqn. (iii) can be differentiated with respect to θ and equated to zero for obtaining the condition for minimum P.

i.e.,
$$\frac{dP}{d\theta} = \frac{d}{d\theta} \left[2 \frac{\sqrt{A}}{\sqrt{\tan \theta}} (\sec \theta) \right] = 0$$
$$= 2\sqrt{A} \left[\frac{\sqrt{\tan \theta} \times \sec \theta \cdot \tan \theta - \sec \theta \times \frac{1}{2} (\tan \theta)^{-1/2} \sec^2 \theta}{\tan \theta} \right] = 0$$
$$= 2\sqrt{A} \left[\frac{\sec \theta \tan \theta}{\sqrt{\tan \theta}} - \frac{\sec^3 \theta}{2(\tan \theta)^{3/2}} \right] = 0$$
or, sec $\theta(2\tan^2 \theta - \sec^2 \theta) = 0$ Since sec $\theta \neq 0$,
 $\therefore 2\tan^2 \theta - \sec^2 \theta = 0$ or $2\tan^2 \theta = \sec^2 \theta$

12. The runway speed of a turbine is(a) The actual running speed at design load	17. The motion of air mass in a tornado is a
(b) The synchronous speed of the generator	(a) Free vortex motion
(c) The speed attained by the turbine under no	(b) Forced vortex motion
load condition	(c)Free vortex at center and forced vortex
(d)The speed of the wheel when governor fails	outside
	(d)Forced vortex at centre and free vortex
13. In the selection of turbine by specific speed or head, which one of the following statements	outside
in not correct? (a) For specific speed 10-35, Kaplan turbines	18. Flow at constant rate through a tapering pipe is
(b) For specific speed 60-300, Francis turbines	(a) Steady and uniform flow
(c) For head 50-150m, Francis turbine	(b) Steady and non-uniform flow
(d) For head above 300m, Pelton wheel	(c) Unsteady and uniform flow
14. Which of the following fluids can be classified as non-Newtonian?	(d) Unsteady and non-uniform flow19.The pressure intensity is same in all
(a) Kerosene oil and Diesel oil	directions at a point in a fluid
(b) Human blood and Toothpaste	(a)Only when fluid is frictionless and
(c) Diesel oil and water	incompressible
(d) Kerosene and water	(b)Only when fluid is frictionless and is at rest
	(c)Only when fluid is frictionless
15. When an ideal fluid flows past a sphere(a) Highest intensity of pressure occurs around	(d)When there is no relative motion of one fluid layer relative to other
the circumference at right angles to direction of	20. If the capillary rise of water in 1mm
flow. (b)Lowest pressure intensity occurs at front	diameter tube in 3cm, the height of capillary rise of water in a 0.2mm diameter tube in centimeter will be
stagnation point	(a) 1.5 (b) 7.5
(c)Lowest pressure intensity occurs at rear	(c) 15 (d) 75
stagnation point	21. A ship's model of scale 1: 100 had a wave
(c)Total drag is zero	resistance of 1N at its design speed. The
16. Apart from inertial force, which of the	corresponding wave resistance (in N) in
following forces is most important in motion of	prototype will be (a) 100 (b)1000
submarines under water?	(c) 1000000 (d) 1000
(a) Viscous force	(4) 1000
(b) Gravity force(c) Compressive force	22. An old shaped body weighing 7.5kg and
(d) Surface tension force	occupying 0.01 cubic meter volume will be
(ע) שעוומכל נכווצוטוו וטוכל	

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FLUID MECHANICS

47. The depth of water below the spillway and after hydraulic jump are 1 m and 6 m respectively. The head loss will be(a)1.74 m(b) 6 m(c)1.7 m(d) None of these	 (a) Steady uniformed flow (b) Steady non – uniform flow (c) Unsteady uniform flow (d) Unsteady non – uniform flow
48. A body floats in stable equilibrium (a)When its metacentric height is zero(b)When metacentre is above centre of gravity(c) When is centre of gravity is below its centre of buoyancy(d) None of these	 54. The ratio of hydrostatic stress to the volumetric strain within the elastic range is called (a) Modulus of elasticity (b) Shear modulus of elasticity (c)Both modulus of elasticity and shear modulus of elasticity (d) None of these
 49.A one dimensional flow is one which (a) Is uniform (b)Becomes negative (c) I steady uniform (d) Take place in straight lines 50.Separation of flow occurs when pressure 	 55. The resultant upward pressure of a fluid on a floating body is equal to the weight of the fluid displayed by the body. This definition is according to (a) Buoyancy (b) Equilibrium of a floating body (c) Archimedes principle
gradient (a) Tends to approach zero (b) Becomes negative	(d) Bernoulli's theorem56. A liquid would wet the solid, if adhesion forces as compared to cohesion forces
(c) Changes abruptly(d) Reduces to a value when vapour formation starts	are (a) Less (b) More
 51.Centre of pressure on an inclined plane is (a) All the centroid (b) Above the centroid 	(c) Equal(d) Less at low temperature and more at thigh temperature
 (c) Below the centroid (d) At metacentre 52. Bluff body surface 	57. If 850 kg liquid volume of one cubic meter, then 0.85 represents its (a) Specific weight (b) Specific mass (c) Specific analysis (d) Specific duration
 (a) Is smooth so that friction can be neglected (b) Coincides with streamlines (c) Does not coincide with streamlines 	(c) Specific gravity (d) Specific density58. Which of the following is the unit of kinematic viscosity
(d) Perpendicular to streamlines53. Gradually varied flow is	(a) Pascal (b) Poise (c) Stoke (d) Faraday

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In this type of survey horizontal and vertical angles are -measured with the help of theodolite. A theodolite is a very precise instrument used for measuring horizontal and vertical angles.

The theodolite surveys can be broadly classified into two types:

(i) Traverse survey

In traverse survey, the various stations form a polygon. The horizontal angles are measured with the help of a theodolite, whereas the linear measurements are made with a tape.

(ii) Triangulation survey

In triangulation survey, the lines form a system of triangles. The base line is measured accurately and the lengths of all other lines are computed from the measured angles.

Triangulation is used for establishing control points over extensive areas.



Theodolite surveys are quite accurate.

6. Tacheometric Surveys

(i) In this type of survey a special type of theodolite called as Tacheometer is used, which is fitted with a stadia diaphragm having two horizontal cross hairs in addition to the central horizontal hair.(ii) In tacheometric surveying, horizontal angles, horizontal distances and vertical distances (elevation) are measured with tacheometer.

(iii) Although tacheometric surveys are not very accurate in plane areas, but these are extremely

convenient and gives better result then the-theodolite surveys in rough terrain.

7. Photogrammetric Surveys

(i) Photogrammetry is the science of taking measurements with the help of photographs.

(ii) Photogrammetric surveys are generally used for Topographic mapping of large areas.

(iii) These are extremely usefull for obtaining Topographical details of areas which are difficult to access.

(iv) Photographs are generally taken from an aeroplane. However, for certain areas where suitable sites exist, photographs can be taken from ground-based cameras.

8. EDM Surveys

(i) Trilateration is a type of triangulation in which all the three sides of each triangle are measured accurately with the help EDM instruments.

(ii) Then angles are computed indirectly form the known sides of the triangles. Hence all the sides and angles are determined.



Trilateration is also used for fixing the position of control points like triangulation. With the help of modern EDM instruments, the trilateration is more convenient in. comparison to triangulation and is a major means of control surveys

6.3 PRINCIPLES OF SURVEYING

There are two basic principles of surveying.

SURVEYING

The best way to over come the effect of mistake is to compare several measurements of the same quantity and discard the odd measurement which does not follow any law.

Error

This does not arise due to mistake. Rather, it is due to physical condition of instruments like temperature at the time of measurements of the length of a line & limitations of human eye etc.

1. Error = Measured Value – True Value 2. Correction = True Value – Measured Value Hence, Measured Value + Correction = True Value Measured Value – Error = True Value Thus, Correction = (–) Error

6.4.4 Errors are classified as

(i) Systematic error

(ii) Random error

(i) Systematic Error

(a) Systematic error arises from the source that act in a similar manner on servations.

(b) The method of measurement, the instrument used and the physical conditions at the time of measurement causes systematic error

(c) Expansion of steel tapes, frequency change in electro megnatic distance measurement (EDM) instruments and **collimation in a level**, are few examples of possible source of systematic errors.

(d) Systematic errors are cumulative in nature.

(e) The errors caused by systematic error are eliminated by applying corrections.

(f) Systematic errors are not revealed by taking the same measurement again with the same instruments. The only proper way to check systematic error is remeasure the quantity by an entirely different method using different instruments.

(ii) Random Error

1.Random errors are really all those discrepancies remaining, after the mistakes and systematic errors are removed.

2.It is mainly caused by limitations of observer and instruments, and are random in nature.

Important characteristics of Random Error

(i)Small errors occur more frequently than larger ones.

(ii)Positive and negative errors are equally likely.

(iii)Very large error seldom occurs.

(iv)The characteristics described above are the characteristics of normal distribution curve. Hence mathematical equations based on normal probability distribution are used for such errors.

(v)Random errors are not of much significance for ordinary surveys. However, they are quite important in precise, control surveys.

(vi)Random error of mean is directly proportional to $1/\sqrt{N}$,

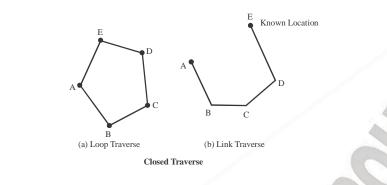
Where N is the no. of observations made.

(vii)For leveling, random error $\propto \sqrt{L}$

Where, L is horizontal length of route.

Units of Measurement

1 ft = 0.3048 m	1 mile = 5280 ft
1 yard = 3 ft	1 mile = 1.609 km
$1 \text{ sq mile} = 2.590 \text{ km}^2$	1 sq mile = 640 acres
1 acre = 43,560 sq ft	1 hectare = $2,471$ acres

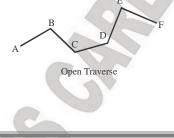


An error in a closed traverse can be easily detected and the traverse can be adjusted and balanced.

6.5.2 Open Traverse

1. An open traverse starts from a station A and closes at another station F whose location is neither known nor established.

- 2. It consists of a series of connected lines.
- 3. An open traverse is generally used in surveying of the area for a road, railway line, canal, etc.

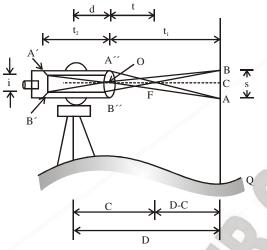


An open traverse cannot be properly checked and adjusted. As far as possible, it should be avoided.

6.5.3 Difference between Traverse Surveying & Chain Surveying

Chain Surveying	Traverse Surveying
1.Requires only linear measure- ments hence relatively easier	1.Requires both linear and angular measurements. Hence requires trained personnel.
2.The frame work consists of triangles	2.Frame work consists of a series of connected lines froming an open or closed polygon. As the directions of lines are measured, the polygon can be plotted without constructing triangles.
3. Check lines are required in chain Surveying	3. Check lines are not required because accuracy of the framework can be-checked by the methods of adjustments.

d is Horizontal distance between optical center O and vertical axis of tacheometer. D is Horizontal distance between staff and vertical axis of tacheometer.



 f_1f_2 is conjugate focal lengths of the lens, and are the distances between the optical centre O and staff, and optical centre O and the image of staff, respectively.

In triangles AOB and A'OB' $\frac{AB}{A'B'} = \frac{OC}{OC''} = \frac{f_1}{f_2} \qquad ...(i)$ $\frac{s}{i} = \frac{f_1}{f_2}$ From the lens formula $\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2} \qquad ...(ii)$ $\frac{f_1}{f_1} = 1 + \frac{f_1}{f_2}$ Substituting for $\frac{f_1}{f_2}$ in eq.(i) $\frac{s}{i} = = \frac{f_1}{f} - 1 \qquad f_1 = \frac{f}{i} s + f \qquad f_1 + d = \frac{f}{i} s + f + d \qquad D = \left(\frac{f}{i}\right) s + (f + d)$

D=Ks+C

1. Above equation is Tacheometric Distance Equation, K and C are the multiplying and additive constants respectively.

2. The multiplying constant $K = \left(\frac{f}{i}\right)$ is also called as stadia interval factor

3.For ease of calculation of distances, the stadia wires are spaced such that the multiplying constant K = 100.

4. The additive constant C = (f + d). Practically speaking, it is a constant value for a tacheometer, because the value of d varies by only a small and negligible amount when focusing the telescope on different objects.

$$R = \frac{15}{\sin D/2}$$

Since for flat curve, D is very small, therefore, $\sin \frac{D}{2} \approx \frac{D}{2}$

$$R = \frac{15}{(D/2) \times \pi/180^{\circ}}; \quad R = \frac{15 \times 2 \times 180^{\circ}}{D \times \pi}$$
$$R = 1718.9/D \approx 1719/D$$

Similarly, for a 20m chord, $\sin \frac{D}{2} = \frac{10}{R}$

$$R = \frac{10}{\sin D/2}$$

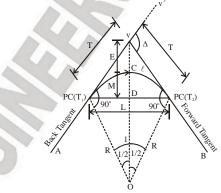
Since for flat curve, D is very small, therefore $\frac{\sin D}{2} \approx \frac{D}{2}$

$$R = \frac{10}{(D/2) \times (\pi/180^{\circ})}$$
$$R = \frac{10 \times 2 \times 180^{\circ}}{D \times \pi}$$
$$R = \frac{1145.9}{D} \approx \frac{1146}{D}$$



For flat curves, a the degree of curve is small, the arc definition and the chord definition given identical results. However, for sharp curves, the two definitions give slightly different results.

6.13.5 Elements of a Simple Circular Curve



1. Length of Curve (*l*) The length of curve T₁CT₂ is given by

of peg A to the centre of the eye-piece is 1.540 m and the reading on peg B is 0.705m. The level is then setup over B. The height of he eye-piece above peg B is 1.490m and a reading on A is 2.195m. The difference in level between A and B is	 (a) By right hand upside down (b) By left hand upright (c) By right hand upright (d) By left hand upside down 28. Check lines (or proof lines) in Chain
(a) 2.900m(b) 3.030m(c) 0.770m(d) 0.785m	 23. Check miles (or proof miles) in chain Surveying are essentially required (a) To plot the chain lines (b) To plot the offsets
24. An internal focusing type surveying telescope may be focused by the movement of	(c) To indicate the accuracy of the survey work(d) To increase the out-turn
(a) Objective glass of the telescope(b) Convex-lens in the telescope(c) Concave lens in the telescope(d) Plano-convex lens in the telescope	29. Correction per chain length of 100 links along a slope of a radians is (a) $100a^2$ (b) $100a$ (c) $100a^3$ (d) $100 a^{(-1)}$
 25. In an adjusted level when the bubble is central, the axis of the bubble tube becomes parallel to (a) Line of sight (b) Line of collimation 	30. If h is the difference in height between end points of a chain of length I the required slope correction is (a) $h^2/(2I)$ (b) $h/(2I)$ (c) h^2/I (d) $h^2/(4I)$
(c) Axis of the telescope(d) None of these	31. Positive error is caused if(a)Length of chain is shorter than the standard
26. The conventional sign shown in the figure below represents a	(b)Slope and sag corrections is not applied(c)Measurements are made along the incorrectly aligned line(d)All options are correct
	32. Prolongation of chain line across an obstruction in chain surveying is done by:(a) Marking angular measurement(b) Drawing perpendiculars with a chain
(a) Road bridge (b) Railway bridge	(c) Solution of triangle(d) All options are correct
(c) Canal bridge (d) Aquaduct	33. Number of links in a 30m metric chain is .
27. For taking offsets with an optical square on the right hand side of the chain line it is held	(a) 100 (b) 150 (c) 180 (d) 200

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(c)Bridge carrying road and railway at the same level(d)A level crossing	(d)Vertical scale comes to an inconvenient position to be read
 69. If the chain line which runs along N-S direction is horizontal and the ground in E-W direction is sloping (a)It is possible to set off sects correctly on east 	 74. The telescope of a dumpy level (a) Is rigidly fixed to the leveling head (b) Can be titled in a vertical plane (c) Can be taken out of its supports and reversed (d) Permits interchange of eye piece and object
side (b)It is possible to set off sets correctly on east	glass
side (c)It is not possible to set off sets correctly on west side	75. The representation of general topography of a very flat terrain is possible only by:(a) Drawing contours at large interval
(d)It is possible to set off sets correctly on both	(b) Drawing contours at small interval
sides	(c) Giving spot levels at large interval
	(d) Giving spot levels to salient features at close
70. What is the psychological widening of a pavement on horizontal curve of radius 230 m for ruling speed 80kmph?(a) 0.455m(b) 0.555	interval76. Which of the following are the required corrections for runway length?
(c) 0.186m (d) 0.136	(a) Correction for elevation
71. If the bearing of $AB = N40^{\circ}W$, bearing of $BC = S70^{\circ}E$, then the value of $\angle ABC$ is (a) 30 degree (b) 70 degree	(b) Correction for gradient(c) Correction for temperature(d) All options are correct
(c) 100 degree (d) None of these	77. A contour canal is
72. Point of tangency is the	(a) Irrigate only on one side(b) Does not needs bank on higher side
(b) End of the curve	(c) Is generally aligned parallel to the counter of
(c) Common point where the radius changes	the area
(d)Common point where the radius and direction changes	(d)All options are correct
73. Left wwing is not much favoured in theodolite survey, because(a)Most of surveyors are accustomed to right hand	78. Which of the following would represent the surface of the water level of a still lake?(a) Level surface(b) Contour surface(c) Horizontal surface(d) None of these
(b)It is inconvenient to turn the telescope anti- clockwise(c) The readings increase clockwise	79. Which of the following leveling is carried out to determine the elevation difference between two points on the surface of earth?(a) Reciprocal leveling

Sol. 105.(d)

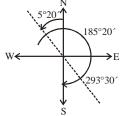
Sol. 106.(d)

Sol. 107.(d)

Sol. 108.(a)

Sol. 109.(d)

Sol. 110.(c)



The sun at noon is $185^{\circ}20'$, the magnetic declination will be $5^{\circ}20'$ west.

Sol. 111.(b)

Sol. 112.(d)

Sol. 113.(c)

Sol. 114.(c)

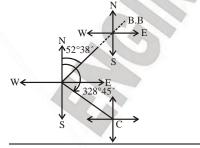
Sol. 115.(b)

L = 6 - 0.8 = 5.2B = 4 - 0.8 = 3.2 = 0.80 × 0.60 × [2 × (5.2 + 3.2)]

Sol. 116.(d)

Sol. 117.(b)

Sol. 118.(d)



LA = $328^{\circ}45' - 52^{\circ}30' = 276^{\circ}15'$ Since it is exterior angle, hence correct answer is $(360 - 276^{\circ}15')$

Sol. 119.(c) $72^{\circ}45'$ $E \leftarrow 287^{\circ}15$

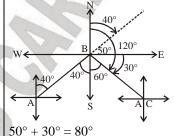
Sol. 120.(a)

Sol. 121.(d)

Sol. 122.(a)

Sol. 123.(a)

Sol. 124.(c)



The included angle between AB and BC is 80° .

Sol. 125.(a)

$$\begin{split} \Sigma Lat_{north} &- \Sigma Lat_{south} = 1m\\ \Sigma Departures_{east} &- \Sigma Departures_{wet} = 1m\\ Resulting closing line in (South West) direction\\ with latitude and departure = 1m\\ Length &= \sqrt{1^2 + 1^2} = \sqrt{2}m \end{split}$$

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